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# ANALYSIS OF THE RELATION BETWEEN LOG SD AND MEAN OF VARIETIES 

Document prepared by experts from Denmark and the United Kingdom

## Introduction

1. At the twenty-eighth session on the Technical Working Party on Automation and Computer Programs, held in Angers, France, from June 29 to July 2, 2010, the bias in the present COYU method was discussed (document TWC/28/27; also previously documents TWC/26/17 and TWC/27/15). One of the possible approaches to overcome the bias in the present method was to use a linear and quadratic adjustment instead of the moving average method. However, it was questioned whether such an adjustment would be appropriate in all cases. It was decided to carry out a survey on the relationship between $\log \mathrm{SD}$ and the mean of varieties in order to see if this could be modelled sufficiently well using a linear or quadratic regression. In such case it would be appropriate to introduce a new method for COYU based on a linear and quadratic effect adjustment of the log SD.
2. The following data were received:

- Data on Lolium perenne (perennial ryegrass) from DE, NL and UK through the years 1993-2002. Part of the data has previous been used in TWC/28/31, A study on Grass Reference Collections in Different Locations.
- Data on Brassica napus L. oleifera (spring oil seed rape) from DK through the years 1997-2005
- Data on Pisum sativum (field pea) from DK through the years 1997-2005

Data

## Lolium perenne from Germany, Netherlands and United Kingdom

3. Data from two groups of oil seed rape grown in DUS trials in Germany, the Netherlands and United Kingdom was examined. Data were available for two subgroups of varieties (Amenity and Forage) for the years 1993 to 2002.

Table 1: Minimum, mean and maximum number of varieties over the combinations of year and country

| Crop | Statistics | UPOV Character number |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 02 | 07 | 08 | 09 | 10 | 11 | 12 | 13 | 14 |
| Lolium perenne, Amenity | Min | 44 | 44 | 44 | 44 | 44 | 44 | 44 | 44 | 52 |
|  | Mean | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 64 | 65 |
|  | Max | 77 | 80 | 74 | 74 | 74 | 74 | 74 | 74 | 73 |
|  |  |  |  |  |  |  |  |  |  |  |
| Lolium perenne, Forage | Min | 35 |  | 34 | 40 | 34 | 34 | 35 | 35 | 35 |
|  | Mean | 57 |  | 57 | 58 | 57 | 57 | 56 | 57 | 57 |
|  | Max | 73 |  | 73 | 73 | 73 | 73 | 73 | 73 | 73 |

4. For Amenity, the UPOV characteristics $02,07,08,09,10,11,12,13$ and 14 were available although some characteristics were not present from all countries. For Forage, the UPOV characteristics $02,08,09,10,11,12,13$ and 14 were available although one characteristic was not present in one country and two characteristics were missing in some years in one country. The number of varieties for each combination of country and year varied between 34 and 74 (see Table 1).

Table 2: Description of the characteristics for Lolium perenne

| UPOV | Description (TG/4/7) | Units |
| :--- | :--- | :--- |
| 02 | Plant: growth habit in autumn of year of sowing | Note |
| 07 | Plant: natural height in spring | cm |
| 08 | Time of inflorescence emergence in 2 ${ }^{\text {nd }}$ year | days |
| 09 | Plant: natural height at inflorescence emergence | cm |
| 10 | Flag leaf: length at inflorescence emergence | mm |
| 11 | Flag leaf: width | mm |
| 12 | Stem : length of longest stem (inflorescence included <br> when fully expanded) | cm |
| 13 | Inflorescence: length | cm |
| 14 | Inflorescence: number of spikelets | no |

${ }^{\text {a) }}$ Recorded as degrees in UK and from this transformed to note using the formula: Note=degree $\times 8 / 90+1$
Brassica napus (spring oil seed rape) and Pisum sativum (field pea) from Denmark
5. Data on reference varieties from two species grown in DUS trials in Denmark was examined. Data were available for the years 1997 to 2005. For Brassica napus, the UPOV characteristics 02, 03, 6, 13, 14, 17, 18, 19 and 20 were used. For Pisum sativum, the UPOV
characteristics $12,13,23,24,25,48$ and 49 were used. The number of varieties for each combination of species and year varied between 64 and 154 (see Table 3).

Table 3: Minimum, mean and maximum number of varieties over the years

| Species | Statistics | UPOV Character number |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 02 | 03 | 06 | 13 | 14 | 17 | 18 | 19 | 20 |
| Brassica napus | Min | 76 | 76 | 65 | 65 | 64 | 65 | 65 | 65 | 65 |
|  | Mean | 97 | 97 | 94 | 94 | 94 | 95 | 94 | 94 | 94 |
|  | Max | 113 | 113 | 112 | 110 | 110 | 111 | 111 | 111 | 111 |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  | UPOV Character number |  |  |  |  |  |  |  |  |
|  |  | 12 | 13 | 31 | 32 | 48 | 49 |  |  |  |
| Pisum sativum | Min | 82 | 82 | 82 | 82 | 82 | 82 |  |  |  |
|  | Mean | 120 | 120 | 120 | 120 | 120 | 120 |  |  |  |
|  | Max | 154 | 154 | 154 | 154 | 154 | 154 |  |  |  |

Table 4: Description of the characteristics for Brassica napus and Pisum sativum

| UPOV | Description (TG/36/6 corr. and TG/7/9) | Units |
| :--- | :--- | :--- |
| Brassica |  | napus L. oleifera (spring oil seed rape) |
| 02 | Cotyledon: length | mm |
| 03 | Cotyledon: width | mm |
| 06 | Leaf: number of lobes | no |
| 13 | Flower: length of petals | mm |
| 14 | Flower: width of petals | mm |
| 17 | Plant: total length including side branches | cm |
| 18 | Siliqua: length | mm |
| 19 | Siliqua: length of beak | mm |
| 20 | Siliqua: length of peduncle | mm |
| Pisum | sativum (field pea) |  |
| 12 | Stem: length. | cm |
| 13 | Stem: number of nodes | no |
| 31 | Stipule. length | mm |
| 32 | Stipule. width | mm |
| 48 | Pod length | mm |
| 49 | Pod: width | mm |

## Method

6. For each combination of crop (or crop subgroup) country, year and characteristic, the data from all varieties was analysed in the following linear regression model:
$Y_{v}=\mu+\alpha_{1} X_{v}+\alpha_{2} x_{v}^{2}+\alpha_{3} X_{v}^{3}+E_{v}$
where
$Y_{v}$ is the $\log$ of the pooled standard deviation for variety $v$
$x_{v}$ is the pooled mean of the observations for variety $v$
$E_{v}$ is the residual (random) variation not explained by the model. It was assumed that the residual term was normally distibuted with mean zero and constant variance.
$\mu$ is the intercept
$\alpha_{1}, \alpha_{2}$ and $\alpha_{3}$ is the linear, quadratic and cubic effect of the mean
After fitting the model the following three tests were performed:
7. Is $\alpha_{1}$ significant different from zero given that $\mu$ already was included in the model
8. Is $\alpha_{2}$ significant different from zero given that $\mu$ and $\alpha_{1}$ already were included in the model
9. Is $\alpha_{3}$ significant different from zero given that $\mu, \alpha_{1}$ and $\alpha_{2}$ already were included in the model
10. The cubic term is included to check whether a linear or quadratic model is sufficient. The results are summarised by the number of times that each of these tests was significant for each characteristic. In addition, the number of times that at least one of these tests was significant was tabulated.
11. For the characteristics where the overall test for the cubic term was significant all combinations of country and year that had a significant term were plotted. In those plots the fit using a straight line, a $2^{\text {nd }}$ degree polynomial and a $3^{\text {rd }}$ degree polynomial are shown together with the fit using a cubic spline with 4 degrees of freedom.

## Results

9. The numbers of significant linear, quadratic and cubic relations between the logarithms of the pooled standard deviation and the means for each characteristic are shown in Tables 5 and 6 for the two groups of Lolium perenne, Table 7 for Brassica napus and in Table 8 for Pisum sativum.

## Lolium perenne, Amenity

10. For the Amenity group, about $65 \%$ ( 140 out of 214 cases) of the examined combinations showed a significant relationship at the $5 \%$ level for at least one of the 3 terms in the model (recorded as " $\geq 1$ " in the table). In most of these cases the linear term was also significant. The quadratic and cubic terms were also significant in several cases. However some of these may be expected to be type I errors. Looking at the tests for cubic relation in each characteristic one finds that the number of tests for characteristic with UPOV number, $02,08,11$ and 13 exceed the number expected with a significance level of $5 \%$ and given the total number of tests for the characteristics. For the same tests at the $1 \%$ level only characteristics 08 and 11 exceed the limit for the number of tests.

Table 5: Number of significant effects for Lolium perenne: Amenity

| UPOV <br> no | Significant at the 5\% level |  |  |  |  | Significant at the 1\% level |  |  |  | Tests |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | total |  |
| 02 | $9^{*}$ | 3 | $6^{*}$ | 14 | $9^{*}$ | 2 | 0 | 11 | 20 |  |
| 07 | $4^{*}$ | 1 | 1 | 5 | $3^{*}$ | 1 | 1 | 4 | 10 |  |
| 08 | $21^{*}$ | $13^{*}$ | $11^{*}$ | 26 | $16^{*}$ | $10^{*}$ | $6^{*}$ | 22 | 29 |  |
| 09 | $11^{*}$ | 3 | 2 | 13 | $10^{*}$ | 2 | 1 | 13 | 20 |  |
| 10 | $26^{*}$ | $4^{*}$ | 1 | 26 | $23^{*}$ | 2 | 0 | 23 | 29 |  |
| 11 | $17^{*}$ | $6^{*}$ | $6^{*}$ | 20 | $13^{*}$ | $4^{*}$ | $4^{*}$ | 16 | 29 |  |
| 12 | $6^{*}$ | 2 | 1 | 8 | $4^{*}$ | 0 | 0 | 4 | 29 |  |
| 13 | $17^{*}$ | 1 | $5^{*}$ | 18 | $10^{*}$ | 0 | 1 | 10 | 29 |  |
| 14 | $8^{*}$ | 3 | 0 | 10 | $6^{*}$ | 0 | 0 | 6 | 19 |  |
| Sum | 119 | 36 | 33 | 140 | 94 | 21 | 13 | 109 | 214 |  |

${ }^{\text {a) }}$ number of cases where at least one of the three terms were significant
${ }^{\text {b) }}$ the number attached with an asterix exceeds the threshold that can be accepted given the level of significance and total number of tests
11. For UPOV characteristics $02,08,11$ and 13 all combinations of country and years that were significant at the $5 \%$ level are shown graphically in Appendix 1. The figures show that even when the $3^{\text {rd }}$ degree term of the polynomial was significant, the $2^{\text {nd }}$ degree polynomial described the relationship almost as well in many cases. The exceptions seemed to be the relations between Log SD and the mean for characteristic 08 in DE 1997 and 1999 where the top around 50 to 55 days was clearly better described by the $3^{\text {rd }}$ degree polynomial (blue line) than the $2^{\text {nd }}$ degree polynomial (green line). In many cases the $3^{\text {rd }}$ degree polynomial seemed to be rather sensitive to a few extreme observations with low or high means. The cubic spline was in most cases located between the $2^{\text {nd }}$ and the $3^{\text {rd }}$ degree polynomial. In some cases both the spline and the $2^{\text {nd }}$ degree polynomial seemed to describe the relationship almost equally well. However, for some characteristics, such as characteristic 08 in DE 1999 the spline described the relationship better than both the $2^{\text {nd }}$ and $3^{\text {rd }}$ degree polynomial (better than the $2^{\text {nd }}$ degree polynomial at means between 45 and 55 and better that the $3^{\text {rd }}$ degree polynomial at means above 65).

## Lolium perenne, Forage

12. For the Forage group, about $55 \%$ ( 159 out of 213 cases) of the examined combinations showed a significant relationship at the $5 \%$ level for at least one of the 3 terms in the model. In most of these cases the linear term was also significant. The quadratic and cubic terms were also significant in several cases. However some of these may be expected to be type I errors. Looking at the tests for cubic relation in each characteristic, one finds that the number of tests for characteristic with UPOV number, 08 and 14 exceed the number needed for being overall significant at the $5 \%$ level and $1 \%$ level given the total number of tests for the characteristics.

Table 6: Number of significant effects for Lolium perenne: Forage

| UPOV <br> no | Significant at the 5\% level |  |  |  | Significant at the 1\% level |  |  |  | Tests <br> total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ |  |
| 02 | $8^{*}$ | $4^{*}$ | 1 | 11 | $8^{*}$ | 2 | 1 | 10 | 20 |
| 08 | $20^{*}$ | $13^{*}$ | $12^{*}$ | 26 | $18^{*}$ | $10^{*}$ | $8^{*}$ | 24 | 30 |
| 09 | $10^{*}$ | 2 | 0 | 12 | $9^{*}$ | 2 | 0 | 11 | 23 |
| 10 | $28^{*}$ | $4^{*}$ | 3 | 29 | $28^{*}$ | 1 | 0 | 28 | 30 |
| 11 | $24^{*}$ | 2 | 1 | 25 | $20^{*}$ | 0 | 1 | 20 | 30 |
| 12 | $17^{*}$ | 1 | 2 | 19 | $9^{*}$ | 0 | 0 | 9 | 30 |
| 13 | $23^{*}$ | 1 | 3 | 25 | $17^{*}$ | 1 | 0 | 17 | 30 |
| 14 | $9^{*}$ | 1 | $5^{*}$ | 12 | $5^{*}$ | 1 | $3^{*}$ | 8 | 20 |
| Sum | 139 | 28 | 27 | 159 | 114 | 17 | 13 | 127 | 213 |

${ }^{\text {a) }}$ number of cases where at least one of the three terms were significant
${ }^{\text {b }}$ the number attached with an asterix exceeds the threshold that can be accepted given the level of significance and total number of tests
13. For UPOV characteristics 08 and 14 , all combinations of country and years that were significant at the $5 \%$ level are shown graphically in Appendix 2. The figures show that, even when the $3^{\text {rd }}$ degree term of the polynomial was significant, the $2^{\text {nd }}$ degree polynomial described the relationship almost as well as the $3^{\text {rd }}$ degree polynomial in most cases. The exceptions seemed to be the relations between Log SD and the mean for characteristic 08 in the NL (and DE) in 1995 and 1999 where the top around 40 to 50 days was clearly better described by the $3^{\text {rd }}$ degree polynomial (blue line) than the $2^{\text {nd }}$ degree polynomial (green line). Likewise, the $3^{\text {rd }}$ degree polynomial also described the top around 35-45 days better for the same characteristic in UK 1997. For characteristic 14, the $3^{\text {rd }}$ degree polynomial described one variety with very few spikelets better than the $2^{\text {nd }}$ degree polynomial (two different varieties). However, overall the $3^{\text {rd }}$ degree polynomial did not seem to describe the relationship for characteristic 14 much better than the $2^{\text {nd }}$ degree polynomial. Also here the cubic spline was most often located between the $2^{\text {nd }}$ and the $3^{\text {rd }}$ degree polynomial. In some cases the spline was clearly better than both polynomials, e.g. characteristic 11 in UK 1997.

## Brassica napus

14. For Brassica napus, about $80 \%$ ( 65 out of 81 cases) of the examined combinations showed a significant relationship at the $5 \%$ level for at least one of the 3 terms in the model (Table 7). In most of these cases the linear term was also significant. The quadratic and cubic terms were also significant in several cases. However some of these may be expected to be type I errors. Looking at the tests for cubic relation in each characteristic, one finds that the number of tests for characteristic with UPOV number 02 and 03 exceed the number needed for being overall significant at the $5 \%$ level or at the $1 \%$ level given the total number of tests for the characteristics.

Table 7: Number of significant effects for Brassica napus

| UPOV <br> no | Significant at the 5\% level |  |  |  | Significant at the 1\% level |  |  |  | Tests |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | total |
| 02 | $5^{*}$ | 2 | 2 | 7 | $4^{*}$ | 1 | $2^{*}$ | 5 | 9 |
| 03 | $7^{*}$ | 2 | $3^{*}$ | 9 | $5^{*}$ | 0 | 1 | 6 | 9 |
| 06 | $5^{*}$ | 2 | 1 | 5 | $3^{*}$ | $2^{*}$ | 0 | 3 | 9 |
| 13 | 2 | 1 | 1 | 2 | $2^{*}$ | 1 | 1 | 2 | 9 |
| 14 | $5^{*}$ | 2 | 1 | 7 | $4^{*}$ | 0 | 0 | 4 | 9 |
| 17 | $5^{*}$ | 1 | 2 | 8 | $5^{*}$ | 1 | 0 | 6 | 9 |
| 18 | $9^{*}$ | 0 | 1 | 9 | $6^{*}$ | 0 | 0 | 6 | 9 |
| 19 | $9^{*}$ | 1 | 0 | 9 | $9^{*}$ | 1 | 0 | 9 | 9 |
| 20 | $9^{*}$ | 0 | 0 | 9 | $9^{*}$ | 0 | 0 | 9 | 9 |
| Sum | 56 | 11 | 11 | 65 | 47 | 6 | 4 | 50 | 81 |

${ }^{\text {a) }}$ number of cases where at least one of the three terms were significant
${ }^{\text {b) }}$ the number attached with an asterix exceeds the threshold that can be accepted given the level of significance and total number of tests
15. For UPOV characteristics 02 and 03 , all combinations of country and years that were significant at the $5 \%$ or $1 \%$ level are shown in Appendix 3. The figures show that, even when the $3^{\text {rd }}$ degree term of the polynomial was significant, the $2^{\text {nd }}$ degree polynomial described the relationship almost as well as the $3^{\text {rd }}$ degree polynomial in 2001, but in 2004 the $3^{\text {rd }}$ degree polynomial described the relationship better than the $2^{\text {nd }}$ degree polynomial. Again the cubic spline was in most cases located between the $2^{\text {nd }}$ and the $3^{\text {rd }}$ degree polynomial
Pisum sativum
16. For Pisum sativum, about $70 \%$ ( 38 out of 54 cases) of the examined combinations showed a significant relationship at the $5 \%$ level for at least one of the 3 terms in the model. In most of these cases the linear term was also significant. The quadratic and cubic term was also significant in some cases. However, some of these may be expected to be type I errors. Looking at the tests for cubic relation in each characteristic, the number of significant cases did not exceed the number needed for being overall significant at the $5 \%$ level given the total number of tests for any of the characteristics.

Table 8: Number of significant effects for Pisum sativum

| UPOV <br> no | Significant at the 5\% level |  |  |  | Significant at the 1\% level |  |  |  | Tests |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ | Linear | Quadratic | Cubic | $\geq 1^{\text {a }}$ |  |
| 12 | $8^{*}$ | 0 | 0 | 8 | $7^{*}$ | 0 | 0 | 7 | 9 |
| 13 | $7^{*}$ | 2 | 0 | 8 | $5^{*}$ | 0 | 0 | 5 | 9 |
| 31 | $3^{*}$ | 1 | 2 | 5 | $2^{*}$ | 0 | 0 | 2 | 9 |
| 32 | $9^{*}$ | 0 | 1 | 9 | $9^{*}$ | 0 | 0 | 9 | 9 |
| 48 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 9 |
| 49 | $4^{*}$ | $5^{*}$ | 1 | 7 | $3^{*}$ | 1 | 1 | 4 | 9 |
| Sum | 31 | 9 | 4 | 38 | 26 | 1 | 1 | 27 | 54 |

${ }^{\text {a) }}$ number of cases where at least one of the three terms were significant
${ }^{\text {b) }}$ the number attached with an asterix exceeds the threshold that can be accepted given the level of significance and total number of tests
17. For the characteristics with UPOV numbers 31,32 and 49 all combinations of country and years that were significant at the 5\% level are shown in Appendix 4. The figures show that, even when the $3^{\text {rd }}$ degree term of the polynomial was significant, the $2^{\text {nd }}$ degree polynomial described the relationship almost as well as the $3^{\text {rd }}$ degree polynomial except for one or two very extreme values at the end of the scale. It should be considered whether such extreme varieties should be considered as comparable reference varieties for the candidate in question. Again the cubic spline was most often located between the $2^{\text {nd }}$ and the $3^{\text {rd }}$ degree polynomial.

## Discussion and conclusions

18. For most cases a model with a linear and quadratic effect described the relation between Log SD and the mean sufficiently well. In many of the cases where the preferred model included a significant cubic term, this seemed to be caused by a few unusual varieties. The $3^{\text {rd }}$ degree polynomial fit seemed to be strongly influenced by extreme standard deviations particularly for varieties with either low or high means. In such cases it might be questioned whether a model that displaying such sensitivity should be used or whether such extreme varieties should be left out of the model fitting. The cubic spline applied seemed to be less influenced by extreme observations and seemed to describe the relationship at least as well as the $2^{\text {nd }}$ and $3^{\text {rd }}$ degree polynomial. In most cases the cubic spline (with 4 degrees of freedom set) was in most cases located between the $2^{\text {nd }}$ and $3^{\text {rd }}$ degree polynomial. However the cubic spline would be a little more difficult to implement than the polynomial regressions and some technical challenges remain.

## APPENDIX 1

## APPENDICES:

Figures showing the relations between $\log \mathrm{SD}$ and mean for combinations of country, years where the $3^{\text {rd }}$ degree polynomial described the relation significant better than the $2^{\text {nd }}$ degree polynomial. There is a figure for each characteristic where the threshold for the number of significant tests was passed.

## Legends:

Black circles: Plot of individual Log SD versus mean for each variety in the given country and year
Purple line: $\quad$ Fit for the relation between $\log$ SD and mean using a straight line
Green line: $\quad$ Fit for the relation between $\log$ SD and mean using a $2^{\text {nd }}$ degree polynomial
Blue line: $\quad$ Fit for the relation between $\log$ SD and mean using a $3^{\text {rd }}$ degree polynomial
Red line: $\quad$ Fit for the relation between $\log \mathrm{SD}$ and mean using a cubic spline with 2 degrees of freedom

## Appendix I, Amenity



Fig 1.1 Amenity characteristic 02


Fig 1.2 Amenity characteristic 08

Appendix 1, page 3


Fig 1.3 Amenity characteristic 11

Appendix 1, page 4


Fig 1.3 Amenity characteristic 11

Appendix 2, Forage


Fig 2.1 Forage characteristic 08


Fig 2.2 Forage characteristic 14

Appendix 3: Brassica napus


Fig 3.1 Brassica characteristic 02


Fig 3.2 Brassica characteristic 03

## APPENDIX 4

Appendix 4, Pisum sativum


Fig 4.1 Pisum characteristic 31


Fig 4.2 Pisum characteristic 32

DK 2002


Fig 4.3 Pisum characteristic 49

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