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## INTERNATIONAL UNION FOR THE PROTECTION OF NEW VARIETIES OF PLANTS GENEVA

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GLOSSARY OF STATISTICAL TERMS

Document prepared by experts from Australia

#### **Glossary of Statistical Terms**

Alpha (α): Statisticians use the Greek letter alpha to indicate the probability of rejecting the statistical hypothesis tested when in fact, that hypothesis is true. Before conducting any statistical test, it is important to establish a value for alpha. For Plant Breeder's Rights, especially for establishing distinctness, it is expected to set alpha at 0.01. This is the equivalent of asserting that one will reject the hypothesis tested if the obtained statistic is among those that would occur only 1 out of 100 times that random samples are drawn from a population in which the hypothesis is true. If the obtained statistic leads to reject the hypothesis tested, it's not because that the obtained statistic could not have occurred by chance. It's that it is ascertained that the odds of obtaining that statistic by chance only are sufficiently low (one out of hundred) that it reasonable to conclude that the results are not due to chance. Could it be a mistake? Of course it could, but at least the probability of such an error is established before testing the hypothesis. It is exactly equal to the value previously established for alpha.

**Alternative Hypothesis:** In <u>hypothesis</u> testing, the null <u>hypothesis</u> and an alternative hypothesis are put forward. If the data are sufficiently strong to reject the null hypothesis, then the null hypothesis is rejected in favor of an alternative hypothesis. For instance, if the null hypothesis were that  $\mu_1 = \mu_2$  then the alternative hypothesis (for <u>a two-tailed test</u>) would be  $\mu_1 \neq \mu_2$ .

**ANOVA:** This term is an acronym for a procedure entitled Analysis of Variance. This procedure employs the statistic (F) to test the statistical significance of the differences among the obtained MEANS of two or more random samples from a given population. More specifically, using the Central Limit Theorem, one calculates two estimates of a population variance.

- (1) An estimate in which the s square of the obtained means of the several samples is multiplied by n (the size of the samples).
- (2) An estimate that is calculated as the average (mean) of the obtained s squares of the several samples.

The statistic (F) is formed as the ratio of (1) over (2). If this ratio is sufficiently larger than 1, the observed differences among the obtained means are described as being statistically significant.

**Bar graph/Histogram:** A histogram is constructed from a <u>frequency table</u>. The intervals are shown on the X-axis and the number of scores in each interval is represented by the height of a rectangle located above the interval. A bar graph is much like a histogram, differing in that the columns are separated from each other by a small distance. Bar graphs are commonly used for <u>qualitative variables</u>.

**Beta** ( $\beta$ ): Statisticians use the Greek letter beta to indicate the probability of failing to reject the hypothesis tested when that hypothesis is false and a specific alternative hypothesis is true. For a given test, the value of beta is determined by the previously elected value of alpha, certain features of the statistic that is being

calculated (particularly the sample size) and the specific alternative hypothesis that is being entertained. While it is possible to carry out a statistical test without entertaining a specific alternative hypothesis, neither beta nor power can be calculated if there is no specific alternative hypothesis. It is relevant to note here that power (the probability that the test will reject the hypothesis tested when a specific alternative hypothesis is true ) is always equal to one minus beta. (ie. Power = 1 - beta ) See Power.

**Binomial Distribution:** When a coin is flipped, the outcome is either a head or a tail. In this example, the event has two <u>mutually exclusive</u> possible outcomes. For convenience, one of the outcomes can be labeled "success" and the other outcome "failure." If an event occurs N times (for example, a coin is flipped N times), then the binomial distribution can be used to determine the probability of obtaining exactly r successes in the N outcomes. The binomial probability for obtaining r successes in N trials is: where P(r) is the probability of exactly r successes, N is the number of events, and  $\pi$  is the probability of success on any one trial. This formula assumes that the events:

- (a) are dichotomous (fall into only two categories)
- (b) are mutually exclusive
- (c) are independent and
- (d) are randomly selected

**Bivariate Normality:** A particular form of distribution of two variables that has the traditional 'bell' shape (but not all bell-shaped distributions are normal). If plotted in three- dimensional space, with the vertical axis showing the number of cases, the shape would be that of a three-dimensional bell (if the variances on both variables were equal) or a 'fireman's hat' (if the variances were unequal). When perfect bivariate normality obtains, the distribution of one variable is normal for each and every value of the other variable. See also Normal Distribution.

**Central Limit Theorem:** The Central Limit Theorem is a statement about the characteristics of the sampling distribution of means of random samples from a given population. That is, it describes the characteristics of the distribution of values we would obtain if we were able to draw an infinite number of random samples of a given size from a given population and we calculated the mean of each sample.

The Central Limit Theorem consists of three statements:

- [1] The mean of the sampling distribution of means is equal to the mean of the population from which the samples were drawn.
- [2] The variance of the sampling distribution of means is equal to the variance of the population from which the samples were drawn divided by the size of the samples.
- [3] If the original population is distributed normally (i.e. it is bell shaped), the sampling distribution of means will also be normal. If the original population is not normally distributed, the sampling distribution of means will increasingly

approximate a normal distribution as sample size increases. (i.e. when increasingly large samples are drawn)

**Chi-Square:** The statistic  $\chi^2$  (Chi-Square) is what statisticians call an enumeration statistic. Rather than measuring the value of each of a set of items, a calculated value of Chi-Square compares the frequencies of various kinds (or categories) of items in a random sample to the frequencies that are expected if the population frequencies are as hypothesized by the investigator. Chi-square is often used to assess the "goodness of fit" between an obtained set of frequencies in a random sample and what is expected under a given statistical hypothesis. For example, Chi-Square can be used to determine if there is reason to reject the statistical hypothesis that the frequencies in a random sample are as expected when the items are from a normal distribution.

**Coefficient:** A coefficient is a constant used to multiply another value. In the linear <u>transformation</u> Y = 3X + 7, the coefficient "3" is multiplied by the variable X. In the <u>linear combination of means</u>  $L = (2)M_1 + (-1)M_2 + (-1)M_3$  the three numbers in parentheses are coefficients.

Completely Randomised Design: An experimental lay-out where the experimental units are homogenous and the treatments are randomly assigned to the uniform experimental units without any bias. It is the simplest experimental design, which is used in the testing of many horticultural and ornamental crops under greenhouse condition where the experimenter has more control over the experimental units.

Confidence Interval: A confidence interval is a range of values that has a specified probability of containing the <u>parameter</u> being estimated. The 95% and 99% confidence intervals, which have 0.95 and 0.99 probabilities of containing the parameter respectively are most commonly used. If the parameter being estimated were  $\mu$ , the 95% confidence interval might look like the following:

$$12.5 \le \mu \le 30.2$$

What this means is that the interval between 12.5 and 30.2 has a 0.95 probability of containing  $\mu$ .

A confidence interval only has the specified probability of containing the parameter if the sample data on which it is based is the only information available about the value of the parameter. As an extreme example, consider the case in which 1000 studies estimating the value of  $\mu$  in a certain population all resulted in estimates between 25 and 30. If one more study were conducted and if the 95% confidence interval on  $\mu$  were computed (based on that one study) to be:

$$35 \le \mu \le 45$$

Confounding: Two <u>variables</u> are confounded if they vary together in such a way that it is impossible to determine which variable is responsible for an observed effect. For example, consider an experiment in which two fungicides treatments for foliar disease control were compared. Treatment one was given to the one variety and treatment two was given to another variety. If a difference between treatments were found, it would be impossible to tell if one treatment were more

effective than the other or if treatments for disease control are more effective for one variety than the other. In this case, varieties and treatment are confounded. Naturally, no competent experimenter would design an experiment like that. However, some confounding is much more subtle. An experimenter may accidentally manipulate a variable in addition to the variable of interest.

**Consistency:** An <u>estimator</u> is consistent if the estimator tends to get closer to the <u>parameter</u> it is estimating as the <u>sample size</u> increases. All statistics covered in this text are consistent estimators.

**Contingency Table:** A contingency table is a table showing the responses of subjects to one variable as a function of another variable. For instance, the following contingency table shows disease resistance as a function of different varieties (the data are hypothetical). The entries show the number of plants for each variety under different level of disease resistance. The Chi-square test of <u>independence</u> is used to test the relationship between rows (varieties) and columns (disease resistance) for significance.

Variety	Resistant	Moderately	Susceptible
		Resistant	_
Candidate	18	20	2
Comparator 1	3	10	27
Comparator 2	6	24	10

Continuous Variable: A continuous <u>variable</u> is one for which, within the limits the variable ranges, any value is possible. For example, the variable 'plant height' is continuous since it may be 1.21m, 1.25m or even 1.30m etc to measure plant heights. The variable 'Number of lobed leaves' is not a continuous variable since it is not possible to get 54.12 lobed leaves from 100 leaves counted. It must be an integer. A variable that is not continuous is called 'discrete'.

Correlation: Given a pair of related measures (X and Y) on each of a set of items, the correlation coefficient (r) provides an index of the degree to which the paired measures co-vary in a linear fashion. In general r will be positive when items with large values of X also tend to have large values of Y whereas items with small values of X tend to have small values of Y. Correspondingly, r will be negative when Items with large values of X tend to have small values of Y whereas items with small values of X tend to have large values of Y. The value of r is calculated by first converting the Xs and Ys into their respective Z Scores and, keeping track of which Z Score goes with which item, determining the value of the mean Z Score product. Numerically, r can assume any value between -1 and +1 depending upon the degree of the relationship. Plus and minus one indicate perfect positive and negative relationships whereas zero indicates that the X and Y values do not co-vary in any linear fashion.

**Critical Value:** A critical value is used in <u>significance testing</u>. It is the value that a test <u>statistic</u> must exceed in order for the null <u>hypothesis</u> to be rejected. For example, the critical value of  $\underline{t}$  (with 12 <u>degrees of freedom</u> using the 0.05 significance <u>level</u>) is 2.18. This means that for the probability to be less than or equal to 0.05, the absolute value of the t statistic must be 2.18 or greater.

**Degrees of Freedom:** Statisticians use the terms 'degrees of freedom' to describe the number of values in the final calculation of a statistic that are free to vary. Consider, for example the statistic s-square.

To calculate the s-square of a random sample, we must first calculate the mean of that sample and then compute the sum of the several squared deviations from that mean. While there will be n such squared deviations only (n-1) of them are, in fact, free to assume any value whatsoever. This is because the final squared deviation from the mean must include the one value of X such that the sum of all the Xs divided by n will equal the obtained mean of the sample. All of the other (n-1) squared deviations from the mean can, theoretically, have any values whatsoever. For these reasons, the statistic s-square is said to have only (n-1) degrees of freedom.

**Dependent Variable:** A variable which the analyst is trying to explain in terms of one or more independent variables. The distinction between dependent and independent variables is typically made on theoretical grounds-in terms of a particular causal model or to test a particular hypothesis.

**Discrete Variable:** A discrete <u>variable</u> is one that cannot take on all values within the limits of the variable. For example, responses to a five-point rating scale can only take on the values 1, 2, 3, 4, and 5. The variable cannot have the value 1.7. A variable such as a plant height can take on any value. Variables that can take on any value and therefore are not discrete are called <u>continuous</u>. <u>Statistics</u> computed from discrete variables are continuous. The mean on a five-point scale could be 3.117 even though 3.117 is not possible for an individual score.

**Dispersion:** A <u>variable's</u> dispersion is the degree to which scores on the variable differ from each other. If every score on the variable were about equal, the variable would have very little dispersion. There are many measures of dispersion, eg. variance, standard deviation etc.

**Efficiency:** The efficiency of a <u>statistic</u> is the degree to which the statistic is stable from sample to sample. That is, the less subject to <u>sampling fluctuation</u> a statistic is, the more efficient it is. The efficiency of statistics is measured relative to the efficiency of other statistics and is therefore often called the relative efficiency. If statistic A has a smaller <u>standard error</u> than statistic B, then statistic A is more efficient than statistic B. The relative efficiency of two statistics may depend on the distribution involved. For instance, the <u>mean</u> is more efficient than the <u>median</u> for <u>normal distributions</u> but not for many types of <u>skewed</u> distributions. The efficiency of a statistic can also be thought of as the precision of the estimate: The more efficient the statistic, the more precise the statistic is as an estimator of the <u>parameter.</u>

**Estimator:** An estimator is used to estimate a <u>parameter</u>. Normally <u>a statistic</u> is used as an estimator. Three important characteristics of estimators are: <u>bias</u>, <u>consistency</u>, and relative <u>efficiency</u>.

**Expected Value:** A theoretical average value of a statistic over an infinite number of samples from the same population.

**F Distribution:** The F distribution is the distribution of the ratio of two estimates of <u>variance</u>. It is used to compute <u>probability values</u> in the <u>analysis of variance</u>. The F distribution has two parameters: <u>degrees of freedom</u> numerator (dfn) and degrees of freedom denominator (dfd). The dfn is the number of degrees of freedom that the estimate of variance used in the numerator is based on. The dfd is the number of degrees of freedom that the estimate used in the denominator is based on. The dfd is often called the degrees of freedom error or dfe. In the simplest case <u>of a one-factor between-subjects</u> ANOVA,

dfn = a-1

dfd = N-a

where "a" is the number of groups and "N" is the total number of subjects in the experiment. The shape of the F distribution depends on dfn and dfd. The lower the degrees of freedom, the larger the value of F needed to be significant. For instance, if dfn = 4 and dfd = 12, then an F of 3.26 would be needed to be significant at the 0.05 level. If the dfn were 10 and the dfd were 100, then an F of 1.93

**Factor:** A factor is an <u>independent variable</u>. If an experiment is testing the effect of fertiliser dosage, then 'fertiliser' is a factor. Some experiments have more than one factor. For example, if the effect of fertiliser dosage and irrigation water were both manipulated in the same experiment, then these two variables would be factors. The experiment would be called a two-factor experiment.

**Factorial Design:** When an experimenter is interested in the effects of two or more <u>independent variables</u>, it is usually more efficient to manipulate these variables in one experiment than to run a separate experiment for each variable. Moreover, only in experiments with more than one independent variable is it possible to test for <u>interactions</u> among variables. Consider a hypothetical experiment on the effects of nitrogen on grain yield in a cereal crop. There were three <u>levels</u> of nitrogen dosage: 50kg, 100kg and 150kg per hectare. A second variable, water level, was also manipulated. There were two levels of irrigation water on the field: 5cm and 10cm. The grain yield data (t/ha) for each condition in the experiment is shown below:

Dosage	5cm	10cm
50 kg/ha	1.5	1.8
100/ ha	2.5	2.2
150/ ha	2.8	1.9

The number of condition (six) is therefore the product of the number of levels of dosage (three) and level of water (two). Also see: Main Effect.

**Frequency Distribution:** A frequency distribution shows the number of observations falling into each of several ranges of values. Frequency distributions are portrayed as <u>frequency tables</u>, <u>histograms</u>, or <u>polygons</u>. Frequency distributions can show either the actual number of observations falling in each range or the percentage of observations. In the latter instance, the distribution is called a relative frequency distribution.

**Frequency Table:** A frequency table is constructed by dividing the scores into intervals and counting the number of scores in each interval. The actual number of scores as well as the percentage of scores in each interval are displayed.

**Heteroscedasticity:** The absence of homogeneity of variance. See Homogeneity of Variance.

**Hierarchical Analysis:** In the context of multidimensional contingency table analysis, a hierarchical analysis is one in which inclusion of a higher order interaction term implies the inclusion of all lower order terms. For example, if the interaction of two independent variables is included in an explanatory model, then the main effects for both of those variables are also included in the model.

**Homogeneity of Variance:** The assumption of homogeneity of variance is that the <u>variance</u> within each of the <u>populations</u> is equal. This is an assumption of <u>analysis of variance</u> (ANOVA). ANOVA works well even when this assumption is violated except in the case where there are unequal numbers of subjects in the various groups. If the variances are not homogeneous, they are said to be heterogeneous.

**Homoscedasticity:** See Homogeneity of Variance.

**Hypothesis Testing:** Hypothesis testing is a method of <u>inferential statistics</u>. An experimenter starts with a hypothesis about a <u>population</u> parameter called the <u>null hypothesis</u>. Data are then collected and the viability of the null hypothesis is determined in light of the data. If the data are very different from what would be expected under the assumption that the null hypothesis is true, then the null hypothesis is rejected. If the data are not greatly at variance with what would be expected under the assumption that the null hypothesis is true, then the null hypothesis is not rejected. Failure to reject the null hypothesis is not the same thing as <u>accepting the null hypothesis</u>.

**Independent Variable:** Two variables are independent if knowledge of the value of one variable provides no information about the value of another variable. For example, if you measured the terminal leaf length and the degree of fragrance in a rose variety, then these two variables would in all likelihood be independent. Knowing that leaf length would not effect the fragrance of rose. However, if the variables were leaf length and leaf width, then there may be a high degree of dependence. When two variables are independent then the <u>correlation</u> between them is 0.

**Interaction:** A situation in which the direction and/or magnitude of the relationship between two variables depends on (i.e., differs according to) the value of one or more other variables. When interaction is present, simple additive techniques are inappropriate; hence, interaction is sometimes thought of as the absence of additivity. Synonyms: non-additivity, conditioning effect, moderating effect, contingency effect.

**Interval Scale:** A scale consisting of equal-sized units. On an interval scale the distance between any two positions is of known size. Results from analytic

techniques appropriate for interval scales will be affected by any non-linear transformation of the scale values. See also Scale of Measurement.

**Intervening Variable:** A variable, which is postulated to be a predictor of one or more dependent variables, and simultaneously predicted by one or more independent variables. Synonym: mediating variable.

**Kurtosis:** Kurtosis indicates the extent to which a distribution is more peaked or flat-topped than a normal distribution.

**Least Significant Difference (LSD):** A commonly used mean separation procedure. The difference between two means are declared significant at any desired level of significance if it exceed the value derived from the following formula:

$$LSD = t (S\sqrt{2}) / \sqrt{n}$$

Where t is the tabulated t-value at the required probability and degrees freedom. S is the standard error of means and n is the number of observations per mean.

**Linear:** The form of a relationship among variables such that when any two variables are plotted, a straight line results. A relationship is linear if the effect on a dependent variable of a change of one unit in an independent variable is the same for all possible such changes.

**Linear Regression:** Linear regression is the prediction of one <u>variable</u> from another variable when the relationship between the variables is assumed to assumed to be <u>linear</u>.

**Linear Transformation:** A linear transformation of a variable involves multiplying each value of the variable by one number and then adding a second number. For example, consider the variable X with the following three values: 2, 3, and 7. One linear transformation of the variable would be to multiply each value by 2 and then to add 5. If the transformed variable is called Y, then Y = 2X+5. The values of Y are: 9, 11 and 19.

**Main Effect:** The main effect of an independent <u>variable</u> is the effect of the variable averaging over all <u>levels</u> of other variables in the experiment. The main effect of irrigation water given in Factorial Design example could be assessed by computing the mean for the two levels of water averaging across all three levels of nitrogen dosage. The mean for the 5cm water is: (1.5 + 2.5 + 2.8)/3 = 2.27 and the mean for the 10cm water is: (1.8 + 2.2 + 1.9)/3 = 1.97. The main effect of water, therefore, involves a comparison of the mean of the 5cm water (2.27) with the mean of the 10cm water (1.97). <u>Analysis of variance</u> provides a <u>significance</u> test for the main effect of each variable in the design.

**Mean:** The arithmetic mean is what is commonly called the average. When the word "mean" is used without a modifier, it can be assumed that it refers to the arithmetic mean. The mean is the sum of all the scores divided by the number of scores. The formula in <u>summation notation</u> is:  $\mu = X/N$ , where  $\mu$  is the <u>population</u> mean and N is the number of scores. If the scores are from a <u>sample</u>, then the symbol M refers to the mean and N refers to the <u>sample size</u>. The formula

for M is the same as the formula for  $\mu$ . The mean is a good measure of <u>central tendency</u> for roughly symmetric distributions but can be misleading in <u>skewed</u> distributions since it can be greatly influenced by extreme scores. Therefore, other statistics such as the <u>median</u> may be more informative for distributions such as reaction time or family income that are frequently very skewed. The sum of squared deviations of scores from their mean is lower than their squared deviations from any other <u>number</u>. For <u>normal distributions</u>, the mean is the most <u>efficient</u> and therefore the least subject to <u>sample fluctuations</u> of all measures of central tendency.

**Mean Square Error:** The mean square error (MSE) is an estimate of the population variance in the <u>analysis of variance</u>. The mean square error is the denominator of the F ratio.

**Median:** The median is the middle of a distribution: half the scores are above the median and half are below the median. The median is less sensitive to extreme scores than the <u>mean</u> and this makes it a better measure than the mean for highly skewed distributions.

**Measure of Association:** A number (a statistic) whose magnitude indicates the degree of correspondence-ie, strength of relationship-between two variables. An example is the Pearson product-moment correlation coefficient. Measures of association are different from statistical tests of association (e.g., Pearson chisquare, F test) whose primary purpose is to assess the probability that the strength of a relationship is different from some pre-selected value (usually zero). See also Statistical Measure, Statistical Test.

**Missing Data:** Information that is not available for a particular case for which at least some other information is available.

**Mode:** The mode is the most frequently occurring score in a distribution and is used as a measure of <u>central tendency</u>. The advantage of the mode as a measure of central tendency is that its meaning is obvious. Further, it is the only measure of central tendency that can be used with <u>nominal</u> data. The mode is greatly subject to <u>sample fluctuations</u> and is therefore not recommended to be used as the only measure of central tendency. A further disadvantage of the mode is that many distributions have more than one mode. These distributions are called "multimodal." In a <u>normal distribution</u>, the <u>mean</u>, <u>median</u>, and mode are identical.

**Mutually Exclusive Events:** Two events are mutually exclusive if it is not possible for both of them to occur. For example, if a die is rolled, the event "getting a 1" and the event "getting a 2" are mutually exclusive since it is not possible for the die to be both a one and a two on the same roll. The occurrence of one event "excludes" the possibility of the other event.

**Multivariate Normality:** The form of a distribution involving more than two variables in which the distribution of one variable is normal for each and every combination of categories of all other variables. See also Normal Distribution.

**Nominal Scale:** A classification of cases which defines their equivalence and non-equivalence, but implies no quantitative relationships or ordering among

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them. Analytic techniques appropriate for nominally scaled variables are not affected by any one-to-one transformation of the numbers assigned to the classes. See also Scale of Measurement.

Nonadditive: Not additive. See Interaction.

**Normal Distribution:** A particular form for the distribution of a variable which, when plotted, produces a 'bell' shaped curve- symmetrical, rising smoothly from a small number of cases at both extremes to a large number of cases in the middle. Not all symmetrical bell-shaped distributions meet the definition of normality

**Normality:** See Normal Distribution.

**Null Hypothesis:** The null hypothesis is an hypothesis about a population parameter. The purpose of <u>hypothesis testing</u> is to test the viability of the null hypothesis in the light of experimental data. Depending on the data, the null hypothesis either will or will not be rejected as a viable possibility. Consider a researcher interested in whether the Variety 1 is taller than Variety 2. The null hypothesis is that  $\mu_1$  -  $\mu_2$  = 0 where  $\mu_1$  is the mean height of Variety 1 and  $\mu_2$  is the mean height of Variety 2. Thus, the null hypothesis concerns the parameter  $\mu_1$  -  $\mu_2$  and the null hypothesis is that the parameter equals zero. The null hypothesis is often the reverse of what the experimenter actually believes; it is put forward to allow the data to contradict it. In the experiment, the experimenter probably expects that Variety 1 is taller than Variety 2. If the experimental data show that Variety 1 has a sufficiently higher plant height, then the null hypothesis that there is no difference in plant height can be rejected.

**Ordinal Scale:** A classification of cases into a set of ordered classes such that each case is considered equal to, greater than, or less than every other case. Analytic techniques appropriate for ordinally scaled variables are not affected by any monotonic transformation of the numbers assigned to the classes. See also Scale of Measurement.

**Outlying Case (Outlier):** A case whose score on a variable deviates substantially from the mean (or other measure of central tendency). Such cases can have disproportionately strong effects on statistics.

**Parameter:** A parameter is a numerical quantity measuring some aspect of a <u>population</u> of scores. For example, the mean is a measure of <u>central tendency</u>. Greek letters are used to designate parameters. Following are some examples of parameters of great importance in statistical analyses and the Greek symbol that represents each one. Parameters are rarely known and are usually estimated by <u>statistics</u> computed in <u>samples</u>. To the right of each Greek symbol is the symbol for the associated statistic used to estimate it from a sample.

Quantity	Parameter	Statistic
Mean	μ	M
Standard deviation	σ	S
Proportion	$\pi$	p
Correlation	ρ	r

**Pattern Variable:** A nominally scaled variable whose categories identify particular combinations (patterns) of scores on two or more other variables.

**Population:** A population consists of an entire set of objects, observations, or scores that have something in common. For example, a population may include all individual plants that constitute a plant variety. The distribution of a population can be described by several <u>parameters</u> such as the <u>mean</u> and <u>standard deviation</u>. Estimates of these parameters taken from a sample are called <u>statistics</u>.

**Power:** Power is the probability of correctly rejecting a false <u>null hypothesis</u>. Power is therefore defined as:  $1 - \beta$  where  $\beta$  is the <u>Type II error</u> probability. If the power of an experiment is low, then there is a good chance that the experiment will be inconclusive. That is why it is so important to consider power in the design of experiments. There are <u>methods for estimating the power</u> of an experiment before the experiment is conducted. If the power is too low, then the experiment can be redesigned by changing one of the <u>factors that determine power</u>.

**Probability Value:** In <u>hypothesis testing</u>, the probability value (sometimes called the p value) is the probability of obtaining a <u>statistic</u> as different from or more different from the <u>parameter</u> specified in the null <u>hypothesis</u> as the statistic obtained in the experiment. The probability value is computed assuming the null hypothesis is true. If the probability value is below the <u>significance level</u> then the null hypothesis is rejected.

**Random Sampling:** In random sampling, each item or element of the population has an equal chance of being chosen at each draw. A sample is random if the method for obtaining the sample meets the criterion of randomness (each element having an equal chance at each draw). The actual composition of the sample itself does not determine whether or not it was a random sample.

**Randomized Complete Block Design:** An experimental lay-out where the experimental units are heterogeneous. Blocking is done to make the experimental units more homogeneous within each group. Treatments are randomly assigned within each block to minimize the confounding effect of the heterogeneous experimental units. This is a common design for field trials of agricultural crops.

**Range:** The range is the simplest measure of <u>spread</u> or <u>dispersion</u>: It is equal to the difference between the largest and the smallest values. The range can be a useful measure of spread because it is so easily understood. However, it is very sensitive to extreme scores since it is based on only two values. The range should almost never be used as the only measure of spread, but can be informative if used as a supplement to other measures of spread such as the <u>standard deviation</u> or <u>semi-interquartile range</u>. e.g. The range of the numbers 1, 2, 4, 6,12,15,19, 26 = 26 - 1 = 25.

**Range Test:** Range tests are used to compare each mean in an experiment with each other mean; they are based on the <u>studentized range distribution</u>. The most

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commonly used range tests are: Duncan's Multiple range Test, Student-Newman-Keul's Test, Tukey's Test.

**Ranks:** The expression of a particular characteristics (e.g., plant height) relative to other cases on a defined scale-as in 'Short,' 'Medium,' 'Tall' etc. Note that when the actual values of the numbers designating the relative positions (the ranks) are used in analysis they are being treated as an interval scale, not an ordinal scale. See also Interval Scale, Ordinal Scale.

**Ratio Scale:** Ratio scales are like <u>interval scales</u> except they have true zero points. A good example is the Kelvin scale of temperature. This scale has an absolute zero. Thus, a temperature of 300 Kelvin is twice as high as a temperature of 150 Kelvin.

**Regression Line:** A regression line is a line drawn through a <u>scatter-plot</u> of two variables, one is the independent variable (Y) and the other is the dependent variable. The line is chosen so that it comes as close to the points as possible. In linear regression, Y values are obtained from several populations, each population being determined by a corresponding X value. The randomness of Y is essential and it is assumed that the Y populations normal and have a common variance.

**Sample:** A sample is a subset of a <u>population</u>. Since it is usually impractical to test every member of a population, a sample from the population is typically the best approach available. <u>Inferential statistics</u> generally require that sampling be <u>random</u> although some types of sampling seek to make the sample as representative of the population as possible by choosing the sample to resemble the population on the most important characteristics.

**Sample Size:** The sample size is very simply the size of the sample. If there is only one sample, the letter "N" is used to designate the sample size. If samples are taken from each of "a" populations, then the small letter "n" is used to designate size of the sample from each population. When there are samples from more than one population, N is used to indicate the total number of subjects sampled and is equal to (a)(n). If the sample sizes from the various populations are different, then  $n_1$  would indicate the sample size from the first population,  $n_2$  from the second, etc. The total number of subjects sampled would still be indicated by N. When <u>correlations</u> are computed, the sample size (N) refers to the number of subjects and thus the number of pairs of scores rather than to the total number of scores. The symbol N also refers to the number of subjects in the formulas for testing differences between <u>dependent means</u>. Again, it is the number of subjects, not the number of scores.

**Sampling Fluctuation:** Sampling fluctuation refers to the extent to which <u>a statistic</u> takes on different values with different samples. That is, it refers to how much the statistic's value fluctuates from <u>sample</u> to sample. A statistic whose value fluctuates greatly from sample to sample is highly subject to sampling fluctuation.

**Scale of Measurement:** Scale of measurement refers to the nature of the assumptions one makes about the properties of a variable; in particular, whether

that variable meets the definition of nominal, ordinal, or interval measurement. See also Nominal Scale, Ordinal Scale, Interval Scale.

Semi-Interquartile Range: The semi-interquartile range is a measure of <u>spread</u> or <u>dispersion</u>. It is computed as one half the difference between the 75th <u>percentile</u> [often called (Q3)] and the 25th percentile (Q1). The formula for semi-interquartile range is therefore: (Q3-Q1)/2. Since half the scores in a distribution lie between Q3 and Q1, the semi-interquartile range is 1/2 the distance needed to cover 1/2 the scores. In a symmetric distribution, an interval stretching from one semi-interquartile range below the median to one semi-interquartile above the median will contain 1/2 of the scores. This will not be true for a <u>skewed</u> distribution, however. The semi-interquartile range is little affected by extreme scores, so it is a good measure of spread for skewed distributions. However, it is more subject to <u>sampling fluctuation</u> in <u>normal</u> distributions than is the <u>standard deviation</u> and therefore not often used for data that are approximately normally distributed.

**Significance Level:** In <u>hypothesis testing</u>, the significance level is the criterion used for rejecting the <u>null hypothesis</u>. The significance level is used in hypothesis testing as follows: First, the difference between the results of the experiment and the null hypothesis is determined. Then, assuming the null hypothesis is true, the probability of a difference that large or larger is computed. Finally, this probability is compared to the significance level. If the probability is less than or equal to the significance level, then the null hypothesis is rejected and the outcome is said to be <u>statistically significant</u>. Traditionally, experimenters have used either the 0.05 level (sometimes called the 5% level) or the 0.01 level (1% level), although the choice of levels is largely subjective. The lower the significance level, the more the data must diverge from the null hypothesis to be significant. Therefore, the 0.01 level is more conservative than the 0.05 level. The Greek letter alpha ( $\alpha$ ) is used to indicate the significance level.

**Significance Test:** A significance test is performed to determine if an observed value of a <u>statistic</u> differs enough from a hypothesized value of a <u>parameter</u> to draw the inference that the hypothesized value of the parameter is not the true value. The hypothesized value of the parameter is called the <u>"null hypothesis."</u> A significance test consists of calculating the probability of obtaining a statistic as different or more different from the null hypothesis (given that the null hypothesis is correct) than the statistic obtained in the sample. If this probability is sufficiently low, then the difference between the parameter and the statistic is said to be "statistically significant." Just how low is sufficiently low? The choice is somewhat arbitrary but by convention <u>levels</u> of 0.05 and 0.01 are most commonly used. For instance, in Plant Breeder's Rights the varietal distinctness based on measured characteristics are often tested at 0.01 level.

**Simple Effect:** A simple effect of an <u>independent variable</u> is the effect at a single <u>level</u> of another variable. Often simple effects are computed following a significant interaction.

**Skewness:** Skewness is a measure of lack of symmetry of a distribution.

**Standardized Coefficient:** When an analysis is performed on variables that have been standardized so that they have variances of 1.0, the estimates that result are known as standardized coefficients; for example, a regression run on original variables produces unstandardized regression coefficients known as b's, while a regression run on standardized variables produces standardized regression coefficients known as betas. (In practice, both types of coefficients can be estimated from the original variables.)

**Standard Deviation:** It is the square root of the average squared deviation of each observation from the arithmetic mean. In other words it is the square root of variance See Variance.

**Standard Error:** The standard error of a <u>statistic</u> is the <u>standard deviation</u> of the <u>sampling distribution</u> of that statistic. Standard errors are important because they reflect how much <u>sampling fluctuation</u> a statistic will show. The <u>inferential statistics</u> involved in the construction of <u>confidence intervals</u> and <u>significance testing</u> are based on standard errors. The standard error of a statistic depends on the sample size. In general, the larger the sample size the smaller the standard error. The standard error of a statistic is usually designated by the Greek letter sigma ( $\sigma$ ) with a subscript indicating the statistic. For instance, the standard error of the <u>mean</u> is indicated by the symbol:  $\sigma_M$ .

**Standard Error of Mean:** The <u>standard error</u> of the mean is designated as:  $\sigma_M$ . It is the <u>standard deviation</u> of the <u>sampling distribution</u> of the mean. The formula for the standard error of the mean is:  $\sigma_M = \sigma/\sqrt{N}$ , where  $\sigma$  is the standard deviation of the original distribution and N is the <u>sample size</u> (the number of scores each mean is based upon). This formula does not assume a <u>normal distribution</u>. However, many of the uses of the formula do assume a normal distribution. The formula shows that the larger the sample size, the smaller the standard error of the mean. More specifically, the size of the standard error of the mean is inversely proportional to the square root of the sample size.

**Standard Normal Distribution:** The standard normal distribution is a <u>normal distribution</u> with a <u>mean</u> of 0 and a <u>standard deviation</u> of 1. Normal distributions can be transformed to standard normal distributions by the formula:

$$Z = (X - \mu) / \sigma$$

Where, X is a score from the original normal distribution,  $\mu$  is the mean of the original normal distribution, and  $\sigma$  is the standard deviation of original normal distribution. The standard normal distribution is sometimes called the z distribution.

**Standard Scores:** When a set of scores are converted to <u>z-scores</u>, the scores are said to be standardized and are referred to as standard scores. Standard scores have a mean of 0 and a standard deviation of 1.

**Standardized Variable:** A variable that has been transformed by multiplication of all scores by a constant and/or by the addition of a constant to all scores. Often these constants are selected so that the transformed scores have a mean of zero and a variance (and standard deviation) of 1.0.

**Statistics:** The word "statistics" is used in several different senses. In the broadest sense, "statistics" refers to a range of techniques and procedures for analyzing data, interpreting data, displaying data, and making decisions based on data. This is what courses in "statistics" generally cover. In a second usage, a "statistic" is defined as a numerical quantity (such as the <u>mean</u>) calculated in a <u>sample</u>. Such statistics are used to estimate <u>parameters</u>. The term "statistics" sometimes refers to calculated quantities regardless of whether or not they are from a sample.

**Statistical Independence:** A complete lack of covariation between variables, a lack of association between variables. When used in analysis of variance or covariance, statistical independence between the independent variables is sometimes referred to as a balanced design.

**Statistical Measure:** A number (a statistic) whose size indicates the magnitude of some quantity of interest-e.g., the strength of a relationship, the amount of variation, the size of a difference, the level of income, etc. Examples include means, variances, correlation coefficients, and many others. Statistical measures are different from statistical tests. See also Statistical Test.

**Statistical Significance:** Significance tests are performed to see if the <u>null hypothesis</u> can be rejected. If the null hypothesis is rejected, then the effect found in a <u>sample</u> is said to be statistically significant. If the null hypothesis is not rejected, then the effect is not significant. The experimenter chooses a <u>significance level</u> before conducting the statistical analysis. The significance level chosen determines the probability of a <u>Type I error</u>. A statistically significant effect is not necessarily practically significant.

**Statistical Test:** A number (a statistic) that can be used to assess the probability that a statistical measure deviates from some pre-selected value (often zero) by no more than would be expected due to the operation of chance if the cases studied were randomly selected from a larger population. Examples include Pearson chisquare, F test, t test, and many others. Statistical tests are different from statistical measures. See also Statistical Measure.

**t- Test:** A t-test is any of a number of tests base on the <u>t distribution</u>. The general formula for t is:

t = (statistic – hypothesised value)/ estimated standard error of statistic

The most common t-test is a test for a difference between two means.

**Trimmed Mean:** A trimmed mean is calculated by discarding a certain percentage of the lowest and the highest scores and then computing the mean of the remaining scores. For example, a mean trimmed 50% is computed by discarding the lower and higher 25% of the scores and taking the mean of the remaining scores. The <u>median</u> is the mean trimmed 100% and the arithmetic <u>mean</u> is the mean trimmed 0%. A trimmed mean is obviously less susceptible to the effects of extreme scores than is the arithmetic mean. It is therefore less

susceptible to sampling <u>fluctuation</u> than the mean for <u>skewed</u> distributions. It is less efficient than the mean for normal

**Transformation:** A change made to the scores of all cases (e.g., persons) on a variable by the application of the same mathematical operation(s) to each score. (Common operations include addition of a constant, multiplication by a constant, taking logarithms, arcsine, ranking, bracketing, etc.)

**Two-Point Scale:** If each case is classified into one of two categories (e.g., present/absent, tall/dwarf, dead/alive) the variable is a two-point scale. For analytic purposes, two-point scales can be treated as nominal scales, ordinal scales, or interval scales.

Type I and Type II Error: There are two kinds of errors that can be made in significance testing: (1) a true null hypothesis can be incorrectly rejected and (2) a false null hypothesis can fail to be rejected. The former error is called a Type I error and the latter error is called a Type II error. These two types of errors are defined in the following table. The probability of a Type I error is designated by the Greek letter alpha ( $\alpha$ ) and is called the Type I error rate; the probability of a Type II error (the Type II error rate) is designated by the Greek letter beta ( $\beta$ ). A Type II error is only an error in the sense that an opportunity to reject the null hypothesis correctly was lost. It is not an error in the sense that an incorrect conclusion was drawn since no conclusion is drawn when the null hypothesis is not rejected.

STATISTICAL	H <sub>o</sub> True	H <sub>o</sub>
DECISION		False
Reject H <sub>o</sub>	Type I error	Correct
Do not Reject H <sub>o</sub>	Correct	Type II error

**Variable:** A variable is any measured characteristic or attribute that differs for different subjects. For example, if the height of 30 plants were measured, then height would be a variable. Variables can be quantitative or qualitative. (Qualitative variables are sometimes called "categorical variables.") Quantitative variables are measured on an <u>ordinal</u>, <u>interval</u>, or <u>ratio</u> scale; qualitative variables are measured on a nominal scale.

**Variability:** A <u>variable's</u> variability is the degree the scores on the variable differ from each other. If every score on the variable were about equal, the variable would have very little dispersion. There are many measures of <u>variability</u>. Dispersion and spread are synonyms for variability.

**Variance:** The variance is a measure of how <u>spread</u> out a distribution is. It is computed as the average squared deviation of each observation from its arithmetic mean. Standard deviation is measured as the square root of variance. Both variance and standard deviation are measures of dispersion of data.

Weighted Data: Weights are applied when one wishes to adjust the impact of cases (e.g., persons) in the analysis, e.g., to take account of the number of

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population units that each case represents. In sample surveys weights are most likely to be used with data derived from sample designs having different selection rates or with data having markedly different subgroup response rates.

**Z Distribution:** The standard normal distribution is sometimes called the z distribution. see Standard Normal Distribution.

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